## Keynesian M odel

## Introduction and Description

This lesson establishes fundamental macro concepts. The Keynesian model is the simplest macro model and is the starting point from the national income accounting identity: GDP $=\mathrm{C}+\mathrm{I}+\mathrm{G}+\mathrm{NX}$. The lesson describes the equilibrium between production and planned expenditures, and investigates the way economic agents react when planned expenditures do not equal production. The consumption function is presented and this leads to a discussion of average and marginal propensities to consume. The discussion then turns to the impact on the equilibrium if consumption or government spending changes.

Activity 19 gives the students practice using the Keynesian model, finding the equilibrium income and understanding the relationship among the concepts of income, consumption and saving. The students calculate APS, APC, M PS and M PC in Activity 20 and see the relationship among those concepts. The students practice calculating various multipliers and using the multiplier concept in Activity 21.

## Objectives

1. Develop the Keynesian model.
2. Explain the four sectors of the Keynesian model.
3. Explain equilibrium in the Keynesian model.
4. Explain the economy's response if income is not at the equilibrium level.
5. Explain the difference between equilibrium output and full-employment output.
6. Explain the consumption function.
7. Describe the relationship between average and marginal propensities to consume and save.
8. Explain the multiplier process.

## Time required

Four class periods or 180 minutes

## Materials

1. Activities 19,20 and 21
2. Visuals 3.1, 3.2, 3.3 and 3.4

## Procedure

1. Tell the students the purpose of the lesson is to develop a simple model of the economy. Start with the national income identity: GDP $=\mathrm{C}+\mathrm{I}+\mathrm{G}+\mathrm{NX}$. By definition, this is always true. From here, planned aggregate expenditures are equal to the sum of planned consumption, planned investment, government spending and net exports. Planned consumption ( C ), government spending $(\mathrm{G})$ and net exports(NX) always occur. Planned investment (I) does not necessarily occur. Sometimes inventories accumulate more than businesses planned, and sometimes businesses draw down inventories more than planned.
2. UseVisual 3.1 to explain the Keynesian model. Note: The price level is held constant in this model. Point out the following:
(A) The $45^{\circ}$ line shows all of the points where real GDP = planned aggregate expenditure.
(B) Equilibrium is the intersection of the $45^{\circ}$ line and the $C+I+G+N X$ line.
(C) Equilibrium does not have to be at fullemployment real GDP.
3. Next discuss equilibrium and disequilibrium in the Keynesian model. Project Visual 3.2. The equilibrium output level is Y. Here aggregate expenditures equal output. At $Y_{1}$, the total output produced is $O B$ and the total expenditures are $O A . O B$ is greater than $O A$; therefore, more is produced than is demanded. Firms experience a build-up of inventories: M ore product is unsold and sitting in the warehouse. Firms will respond by producing less and usually laying off workers.

The output will decrease and move the economy toward the equilibrium level of output Y.
4. Now draw a vertical line at a level of output below Y. Ask the students to explain what is going on in the economy. M ore is demanded than is supplied; firms will be experiencing unplanned inventory reduction. Firms will respond by increasing production and employment. The economy will move toward Y .
5. Now look at one component of aggregate expenditures: consumption. Explain that consumption can be represented by the equation $C=a+b Y$, where $Y$ is income or output. The $b$ is the marginal propensity to consume (M PC). It shows the amount by which consumption will increase if income increases by \$1. M PC = change in consumption / change in income.
6. H ave the students complete Activity 19, and review the answers.
7. In the simplest model, households have only two things they can do with their income: consume or save. Thus, $Y=C+S$. Use Visual 3.3 to show savings and dissavings. In addition, since households have the choice only to consume or save, the marginal propensity to consume plus the marginal propensity to save must equal 1, or $M P C+M P S=1$.
8. Have the students complete Activity 20 , and review the answers.
9. Use Visual 3.4 to show what happens if businesses decide to spend more on investment goods. Point out that output goes up. By how much does output rise? Explain the multiplier process to the students. Demonstrate that the result depends on the M PC.
10. Expand on the idea of consumption and make it more realistic by introducing the concept of taxes. The consumption relationship now becomes $\mathrm{C}=\mathrm{a}+\mathrm{bYD}$, where YD is disposable income. Disposable income $=\mathrm{Y}-\mathrm{T}$ where T represents taxes. Thus, households have three ways to spend income: consume, save and pay taxes.
11. Note that if the students are good at al gebra, you can show them how to find the different multipliers by using the following simple equation system and substituting
$C=a+b(Y-T)$
$I=I_{0}$
$G=G_{0}$
$N X=N X_{0}$
$Y=C+I+G+N X$
Here's how to derive the various multipliers:
Substitute the values for C, I, G and NX into the equilibrium condition:
$\mathrm{Y}=\mathrm{a}+\mathrm{b}(\mathrm{Y}-\mathrm{T})+\mathrm{I}_{0}+\mathrm{G}_{0}+\mathrm{NX} \mathrm{X}_{0}$
Collecting like terms, we have:
$\mathrm{Y}-\mathrm{bY}=\mathrm{a}-\mathrm{bT}+\mathrm{I}_{0}+\mathrm{G}_{0}+N \mathrm{X}_{0}$
Solving for Y , we have:
$Y=\frac{a}{(1-b)}-\frac{b T}{(1-b)}+\frac{I_{0}+G_{0}+N X_{0}}{(1-b)}$
Holding T, G and NX constant, a change in I will changeY by
$\Delta Y=(1 /[1-b]) \Delta l$
We then arrive at the investment multiplier:
$\frac{\Delta Y}{\Delta \bar{l}}=\frac{1}{(\overline{1}-\bar{b})}$
Likewise we can derive the lump-sum tax multiplier and arrive at
$\frac{\Delta Y}{\Delta T}=\frac{-\bar{b}}{(1-\mathrm{b})}$
12. H ave the students complete Activity 21 , and review the answers.

## Keynesian Equilibrium

This activity is designed to give you practice with manipulations of the aggregate expenditure model. It shows you how the expenditure schedule is derived and how it helps to determine the equilibrium level of income. This activity assumes that the price level is constant with the consumer price index or price level having a value of 100. All numbers in Figure 19.1 are in billions of constant dollars.

Figure 19.1
Income-Expenditure Schedule

| Income |
| :---: |
| (Output) |


| Consumption |
| :---: |
| Spending |


| Investment <br> Spending | Government <br> Spending | Total Spending <br> (Aggregate <br> Expenditure) |  |  |
| :---: | :---: | :---: | :---: | :---: |
| $\$ 2,400$ | $\$ 2,500$ | $\$ 300$ | $\$ 100$ | $\$ 2,900$ |
| 2,600 | 2,600 | 300 | 100 | $\mathbf{3 , 0 0 0}$ |
| 2,800 | 2,700 | 300 | 100 | $\mathbf{3 , 1 0 0}$ |
| 3,000 | 2,800 | 300 | 100 | $\mathbf{3 , 2 0 0}$ |
| 3,200 | 2,900 | 300 | 100 | $\mathbf{3 , 3 0 0}$ |
| 3,400 | 3,000 | 300 | 100 | $\mathbf{3 , 4 0 0}$ |
| 3,600 | 3,100 | 300 | 100 | $\mathbf{3 , 5 0 0}$ |
| 3,800 | 3,200 | 300 | 100 | $\mathbf{3 , 6 0 0}$ |

1. Use the data on consumption spending and income to draw the consumption function on the graph in Figure 19.2. Label the function C.
2. Using the consumption function you have just drawn and the data on investment and government spending, draw the aggregate expenditure schedule on the same graph. Label it AE ( $C+I+G)$. What is the difference between the aggregate expenditure schedule and the consumption function? \$400: the sum of government spending (G) and investment spending (I)
3. Now draw a line representing all the points at which total spending and income could be equal. Label this the $45^{\circ}$ line.
4. The $45^{\circ}$ line represents all the points that could be the equilibrium level of total spending. Now circle the one point that is the equilibrium level of total spending. What is the equilibrium level of total spending on your graph? $\qquad$ $\$ 3,400$ billion $\qquad$ M

Figure 19.2
Aggregate Expenditure M odel

5. Based on the data in Figure 19.1, and assuming that the full-employment level of total spending is $\$ 3,600$ billion, what conclusions can you draw about the equilibrium level of total spending? The equilibrium level of total spending is below the full-employment level of total spending. There is unemployment of resources; the economy is in a recession.
6. Based on the data in Figure 19.1, and assuming that the full-employment level of total spending is $\$ 3,200$ billion, what conclusions can you draw about the equilibrium level of total spending? The equilibrium level of total spending is above the full-employment level of total spending.
7. If government spending increased by $\$ 100$ billion, what would be the new equilibrium level of total spending? $\qquad$ $\$ 3,600$ billion $\qquad$ For the increase of $\$ 100$ billion in government spending, total spending increased by $\qquad$ $\$ 200$ billion $\qquad$ . Explain why this occurs. Thenew equilibrium level of total spending is $\$ 3,600$ billion. The increase in government spending becomes income to other people who in turn spend a portion of the increase in income, etc. The total effect of the $\$ 100$ billion increase in government spending is an increase in total spending of $\$ 200$ billion.

## Practice with APC, APS, M PC and M PS

## Part A

## Average Propensities

The average propensity to consume (APC) is the ratio of consumption expenditures (C) to disposable income (DI), or APC = C / DI.

The average propensity to save (APS) is the ratio of savings (S) to disposable income, or APS = S/ DI.

1. Using the data in Figure 20.1, calculate the APC and APS at each level of disposable income given. The first calculation is completed as an example.

Figure 20.1
Average Propensities to Consume and to Save

| Disposable Income | Consumption | Saving | APC | APS |
| :---: | :---: | :---: | :---: | :---: |
| \$0 | \$2,000 | -\$2,000 | - | - |
| 2,000 | 3,600 | -1,600 | 1.8 | -0.8 |
| 4,000 | 5,200 | -1,200 | 1.30 | -0.3 |
| 6,000 | 6,800 | -800 | 1.13 | -0.13 |
| 8,000 | 8,400 | -400 | 1.05 | -0.05 |
| 10,000 | 10,000 | 0 | 1.00 | 0 |
| 12,000 | 11,600 | 400 | 0.97 | 0.03 |

2. How can savings be negative? Explain. People are borrowing or reducing their savings to be able to consume at the particular level of income.

## Part B

## Marginal Propensities

The marginal propensity to consume (M PC) is the change in consumption divided by the change in disposable income. It is a fraction of any change in DI that is spent on consumer goods: $\mathrm{MPC}=\Delta \mathrm{C} / \Delta \mathrm{DI}$.

The marginal propensity to save (MPS) is the fraction saved of any change in disposable income. The M PS is equal to the change in saving divided by the change in DI: MPS = $\Delta \mathrm{S} / \Delta \mathrm{DI}$.
3. Using the data in Figure 20.2, calculate the M PC and M PS at each level of disposable income. The first calculation is completed as an example. (This is not a typical consumption function. Its purpose is to provide practice in calculating M PC and M PS.)

Figure 20.2
Marginal Propensities to Consume and to Save

| Disposable Income | Consumption | Saving | MPC | MPS |
| :---: | :---: | :---: | :---: | :---: |
| \$12,000 | \$12,100 | -\$100 | - | - |
| 13,000 | 13,000 | 0 | 0.90 | 0.10 |
| 14,000 | 13,800 | 200 | 0.80 | 0.20 |
| 15,000 | 14,500 | 500 | 0.70 | 0.30 |
| 16,000 | 15,100 | 900 | 0.60 | 0.40 |
| 17,000 | 15,600 | 1,400 | 0.50 | 0.50 |

4. Why must the sum of the M PC and M PS always equal 1? The only choice people have is to consume or to save. Thus an additional dollar in income must result in a change in consumption and/or a change in savings. The sum of the change must beone.

## Part C

Figure 20.3

## Changes in APC and MPC as DI Increases

Disposable

| Income | Consumption | Savings | APC | APS | MPC | MPS |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| \$10,000 | \$12,000 | -\$2,000 | 1.20 | -0.20 | - | - |
| 20,000 | 21,000 | -1,000 | 1.05 | -0.05 | 0.90 | 0.10 |
| 30,000 | 30,000 | 0 | 1.00 | 0 | 0.90 | 0.10 |
| 40,000 | 39,000 | 1,000 | 0.975 | 0.025 | 0.90 | 0.10 |
| 50,000 | 48,000 | 2,000 | 0.96 | 0.04 | 0.90 | 0.10 |
| 60,000 | 57,000 | 3,000 | 0.95 | 0.05 | 0.90 | 0.10 |
| 70,000 | 66,000 | 4,000 | 0.94 | 0.06 | 0.90 | 0.10 |

5. Complete Figure 20.3, and answer the questions based on the completed table.
6. What is the APC at a DI level of $\$ 10,000$ ? $\qquad$ 1.20 At $\$ 20,000$ ? $\qquad$ 1.05
7. What happens to the APC as DI rises? $\qquad$ It decreases,
8. What is the M PC as DI goes from $\$ 50,000$ to $\$ 60,000$ ? $\mathbf{0 . 9 0}$ $\qquad$ From $\$ 60,000$ to $\$ 70,000$ ? $\mathbf{0 . 9 0}$
9. What happens to M PC as income rises? $\qquad$ It remains constant. $\qquad$ What happens to M PS as income rises? $\qquad$ It remains constant.
10. What is the conceptual difference between APC and M PC? The APC measures the average consumption at any level of disposable income. The M PC measures what proportion of each additional dollar of income consumers will spend.

## The M agic of the M ultiplier

The people in Econoland live on an isolated island. One year a stranger arrived and built a factory to make seashell charms. The factory is considered an investment on Econoland. If the marginal propensity to consume on the island were 75 percent, or 0.75, this would mean that Econoland residents would consume or spend 75 percent of any change in income and save 25 percent of any change in income. The additional spending would generate additional income and eventually a multiple increase in income. This is called the multiplier effect. When they heard about this multiplier effect, the islanders were thrilled about the new factory because they liked the idea of additional income.

The residents of Econoland wanted to know what would eventually happen to the levels of GDP, consumption and saving on the island as the new spending worked its way through the economy. Luckily there was a retired university economist who had settled on Econoland who offered a brief statement of the multiplier. "It's simple," he said: "O ne person's spending becomes another person's income." The economist began a numerical example. "This shows the process," he said. The rounds refer to the new spending moving from resident to resident. He stopped his example at four rounds and added the rest of the rounds to cover all Econoland's citizens.

Figure 21.1

## Changes in Econoland's GDP, Consumption and Saving

| Round | Income (GDP) | Consumption Spending | Saving |
| :---: | :---: | :---: | :---: |
| Round 1 | \$1,000 | 0.75 of \$1,000 $=\$ 750$ | 0.25 of \$1,000 = \$250 |
| Round 2 | One person's spending becoming another person's income: \$750 | $\begin{aligned} & 0.75 \text { of } \$ 750 \\ & =\$ 562.50 \end{aligned}$ | $\begin{gathered} 0.25 \text { of } \$ 750 \\ =\$ 187.50 \end{gathered}$ |
| Round 3 | The next person's spending becoming another person's income: $\$ 562.50$ | $\begin{aligned} & 0.75 \text { of } \$ 562.50 \\ & =\$ 421.88 \end{aligned}$ | $\begin{aligned} & 0.25 \text { of } \$ 562.50 \\ & =\$ 140.62 \end{aligned}$ |
| Round 4 | The next person's spending becoming another person's income: \$421.88 | $\begin{aligned} & 0.75 \text { of } \$ 421.88 \\ & =\$ 316.41 \end{aligned}$ | $\begin{aligned} & 0.25 \text { of } \$ 421.88 \\ & =\$ 105.47 \end{aligned}$ |
| Rounds continue |  |  |  |
| All rounds | Final outcome for income (GDP) $1 /(1-0.75) \times \$ 1,000=$ $4 \times \$ 1,000=\$ 4,000$ | Final outcome for consumption spending $0.75 \text { of } \$ 4,000=\$ 3,000$ | Final outcome for saving 0.25 of $\$ 4,000=\$ 1,000$ | na LESSON 1 ■ ACTIVITY 21

Answer Key

The retired economist then summarized the multiplier effect for the assembled crowd of Econolanders. "This shows us that the factory is an investment that has a multiplied effect on our GDP. In this case, the multiplier is 4." He added, "It appears to be magic, but it is simply that one person's spending becomes another person's income." There were some nods of agreement but also many puzzled looks, so the old professor asked the citizens a series of questions. Answer these questions as if you were an Econolander.

1. Would the multiplier be larger or smaller if you saved more of your additional income? Smaller
2. What do you think would happen if all Econolanders saved all of the change in their incomes?

There would not be any change in output from consumption.
3. What would happen if you spent all of the change in your income? There would bean infinite change in output from consumption.

The professor broke out into a smile as the answers all came out correct.
The economist reminded the islanders about the multiplied effect on GDP that a new road around the island would have. That new bridge built by the island government over the lagoon would also have a multiplied effect on GDP. This time there were many more nods of approval and understanding.

The economist also indicated that if the government of Econoland lowered taxes, the citizens would have more income to spend, which would cause a multiplier effect. He said there was another side to this: If the taxes were raised, there would be a multiplier effect, which would decrease income and GDP by a multiple amount.

The King of Econoland commissioned the old economist to write a simple explanation about multipliers so all the citizens of Econoland would understand. He told the old economist: "If you succeed in helping all citizens understand the multiplier in simple terms, you will be rewarded. If not, you will be banished from the island."

The economist started banging away on an old rusting typewriter since he did not want to be banished from this island paradise. The result follows:

## The Professor's Treatise on Multipliers

## M ULTIPLIER FORMULAS AND TERMS

Marginal propensity to consume ( M PC) = change in consumption divided by change in income
M arginal propensity to save (MPS) = change in saving divided by change in income
Investment Multiplier = 1 / (1 - MPC) or simply $1 /$ MPS
How to use the investment multiplier: change in GDP = change in investment times investment multiplier
When to use the investment multiplier: when there is a change in investment such as a new factory or new equipment

Government Spending Multiplier =1/(1-MPC) or simply $1 /$ MPS
How to use the government spending multiplier: change in GDP = change in government spending times government spending multiplier
W hen to use the government spending multiplier: when there is a change in government spending such as a new road or bridge

Tax Multiplier $=-$ MPC $/(1-$ MPC $)=-$ MPC $/$ MPS
How to use the tax multiplier: change in GDP = change in taxes times tax multiplier
W hen to use the tax multiplier: when there is a change in lump-sum taxes. Remember that the tax multiplier has a negative sign.

Figure 21.2

## Multiplier Table

(Derived from using the formulas above)

|  | Investment <br> Multiplier | Government <br> Spending <br> Multiplier | Tax <br> Multiplier |
| :---: | :---: | :---: | :---: |
| 0.90 | 10.0 | 10.0 | -9.0 |
| 0.80 | 5.0 | 5.0 | -4.0 |
| 0.75 | 4.0 | 4.0 | -3.0 |
| 0.60 | 2.5 | 2.5 | -1.5 |
| 0.50 | 2.0 | 2.0 | -1.0 |

## "ALW AYS" RULES (A surefire way to remember multipliers)

- The investment multiplier is always equal to the same value as the government spending multiplier.
- The investment and government spending multipliers are always positive.
- The tax multiplier is always negative.

The King took the treatise and had it printed for every islander. He then ordered the old professor to make up a series of questions to see if the subjects understood the multiplier.

Answer the questions on the professor's test.

## The Econoland Test

1. What is the value of the tax multiplier if the M PC is 0.80 ? $\qquad$ $-4$
2. What is the value of the government spending multiplier if the M PC is 0.67 ? $\qquad$ 3
3. What is the tax multiplier if the M PS is 0.25 ? $\qquad$ $-3$
4. How could the multiplier be used to explain wide swings in income (which could be called business cycles) in Econoland? Small changes in expenditure are magnified by the multiplier effect.
5. The numerical value for the investment and government spending multiplier increases as the
(A) value of the marginal propensity to save decreases,
(B) value of the average propensity to consume increases.
(C) value of the marginal propensity to consume decreases.
(D) value of the marginal propensity to save increases.
(E) value of the average propensity to consume decreases.
6. If the government spending multiplier is 5 in Econoland, the value of the tax multiplier must be
(A) 5
(B) 4
(C) 1
(D) -4
(E) -5

Macroeconomics LESSON 1 ■ ACTIVITY 21

Econoland has the following values for income and consumption. Use this data to answer questions 7, 8 and 9.

| Income | Consumption |
| :--- | :---: |
| 100 | 150 |
| 200 | 225 |
| 300 | 300 |
| 400 | 375 |
| 500 | 450 |
| 600 | 525 |

7. The government spending multiplier in Econoland is
(A) 3
(B) 4
(C) 5
(D) 10
(E) 30
8. If there is an increase in taxes of $\$ 200$ in Econoland, the decrease in GDP will be
(A) $\$ 100$
(B) $\$ 200$
(C) $\$ 400$
(D) $\$ 600$
(E) $\$ 800$
9. If there is an increase in government spending of $\$ 100$ and an increase in taxes of $\$ 100$ in Econoland, then the change in GDP will be
(A) $\$ 50$
(B) $\$ 100$
(C) $\$ 200$
(D) $-\$ 100$
(E) $-\$ 200$
10. Why do the people of Econoland need to understand multipliers? Understanding multipliers allows people to understand the impact of fiscal policy and changes in autonomous components of consumption, investment and government spending on total income.
